Glossary 615

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\mathscr{C}^k
                the space of functions f with \partial^{\alpha} f continuous for all |\alpha| \le k
\mathscr{C}_0
                the space of continuous functions with compact support
                the space of continuous functions that vanish at infinity
\mathscr{C}_{00}
\mathscr{C}_0^{\infty}
                the space of smooth functions with compact support
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                the space of smooth functions with compact support
S.
                the space of Schwartz functions
\mathscr{S}_0
                the space of Schwartz functions \varphi with the property \int_{\mathbb{R}^n} x^{\gamma} \varphi(x) dx = 0
                for all multi-indices \gamma.
\mathscr{C}^{\infty}
                the space of smooth functions \bigcap_{k=1}^{\infty} \mathscr{C}^k
\mathcal{D}'(\mathbf{R}^n)
                the space of distributions on \mathbf{R}^n
\mathscr{S}'(\mathbf{R}^n)
                the space of tempered distributions on \mathbf{R}^n
\mathcal{E}'(\mathbf{R}^n)
                the space of distributions with compact support on \mathbf{R}^n
Đ
                the set of all complex-valued polynomials of n real variables
\mathscr{S}'(\mathbf{R}^n)/\mathscr{P} the space of tempered distributions on \mathbf{R}^n modulo polynomials
\ell(Q)
                the side length of a cube Q in \mathbb{R}^n
\partial Q
                the boundary of a cube Q in \mathbb{R}^n
L^p(X,\mu)
                the Lebesgue space over the measure space (X, \mu)
L^p(\mathbf{R}^n)
                the space L^p(\mathbf{R}^n, |\cdot|)
L^{p,q}(X,\mu)
                the Lorentz space over the measure space (X, \mu)
L_{\mathrm{loc}}^{p}(\mathbf{R}^{n})
                the space of functions that lie in L^p(K) for any compact set K in \mathbb{R}^n
|\mu|
                the total (absolute) variation of a finite Borel measure \mu on \mathbb{R}^n
\mathcal{M}(\mathbf{R}^n)
                the space of all finite (signed) Borel measures on \mathbb{R}^n
\mathcal{M}_p(\mathbf{R}^n)
                the space of L^p Fourier multipliers, 1 \le p \le \infty
\mathcal{M}^{p,q}(\mathbf{R}^n)
                the space of translation-invariant operators that map L^p(\mathbf{R}^n) to L^q(\mathbf{R}^n)
                \int_{\mathbf{R}^n} d|\mu| the norm (total variation) of a finite Borel measure \mu on \mathbf{R}^n
\|\mu\|_{\mathscr{M}}
\mathfrak{M}
                the centered Hardy-Littlewood maximal operator with respect to balls
M
                the uncentered Hardy-Littlewood maximal operator with respect to balls
\mathcal{M}_c
                the centered Hardy-Littlewood maximal operator with respect to cubes
M_c
                the uncentered Hardy-Littlewood maximal operator with respect to
                cubes
\mathcal{M}_{\mu}
                the centered maximal operator with respect to a measure \mu
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